Diffractive Photoproduction of Heavy Vector Mesons at HERA

DISSERTATION

zur Erlangung des Doktorgrades
des Fachbereichs Physik
der Universität Hamburg

vorgelegt von

PETRA MERKEL

aus Hamburg

II. Institut für Experimentalphysik
Universität Hamburg

Hamburg
1999

Gutachter der Dissertation:	Prof. Dr. B. Naroska Prof. Dr. W. Bartel
Gutachter der Disputation:	Prof. Dr. B. Naroska Prof. Dr. A. Wagner
Datum der Disputation:	27.10.1999
Dekan des Fachbereichs Physik und Vorsitzender des Promotionsausschusses:	Prof. Dr. F. W. Büßer

Abstract

Diffractive vector meson production is described on the one hand within the phenomenological framework based on Regge theory, and on the other hand by perturbative QCD calculations. Light vector mesons in the photoproduction regime (where no hard scale is present) agree well with non-perturbative Regge based descriptions. Perturbative effects are measured in the presence of a hard scale for light and for heavy vector mesons. The question arises whether in the case of J/ψ and Υ photoproduction the large mass of the quarks in the mesons provides a sufficiently hard scale in order to apply perturbative QCD.

The aim of this thesis is to clarify this question. In the case of the J/ψ, the energy dependence of the cross section, its t dependence (where t is the four-momentum transfer at the proton vertex), and the energy dependence of the t dependence are measured. The parameters of the exchanged trajectory in the diffractive process – the *pomeron trajectory* – is determined. Finally, the Υ photoproduction cross section is extracted.

All these measurements of diffractive heavy vector meson photoproduction at HERA show good agreement with calculations in perturbative QCD as well as with results from Regge based models under the assumption of a second *hard* pomeron. The exchange of just one *soft* pomeron can be ruled out.

Kurzfassung

Diffraktive Vektormeson Produktion wird einerseits beschrieben im Rahmen phänomenologischer Modelle, die auf der Regge Theorie beruhen, andererseits durch perturbative QCD Rechnungen. Leichte Vektormesonen in Photoproduktion (wo keine harte Skala vorhanden ist) stimmen gut mit nicht perturbativen Vorhersagen Regge basierter Modelle überein. In Gegenwart harter Skalen werden perturbative Effekte sowohl für leichte als auch für schwere Vektormesonen gemessen. Daher erhebt sich die Frage, ob im Fall der J/ψ und der Υ Photoproduktion die große Masse der Quarks in den Mesonen bereits eine genügend harte Skala zur Verfügung stellen, um perturbative QCD anwenden zu können.

Das Ziel dieser Arbeit ist die Klärung dieser Frage. Im Fall des J/ψ wurde die Energieabhängigkeit des Wirkungsquerschnitts, seine t-Abhängigkeit (wobei t der Impulsübertrag am Protonvertex ist) sowie die Energieabhängigkeit der t-Abhängigkeit gemessen. Die Parameter der ausgetauschten Trajektorie in dem diffraktiven Prozeß – die *Pomeron Trajektorie* – wurden erstmals mit den Daten eines einzigen Experiments bestimmt. Schließlich wurde der Υ Photoproduktions Wirkungsquerschnitt extrahiert.

Die Messung all dieser verschiedenen Gesichtspunkte diffraktiver schwerer Vektormeson Photoproduktion bei HERA zeigt gute Übereinstimmung mit Rechnungen in perturbativer QCD und mit Ergebnissen Regge basierter Modelle, unter der Annahme eines zweiten. *harten*, Pomerons. Der Austausch ausschließlich eines *weichen* Pomerons kann ausgeschlossen werden.

Contents

Chapter 1

Introduction

The understanding of the fundamental forces and the elementary particles is the subject of the field of high energy physics. Within the last 20 years the *Standard Model* has been developed and tested in a multitude of experiments. It provides a satisfactory description of all those processes measured in strong, weak and electro-magnetic interactions, for which it is expected to work.

A special type of interactions, so-called *diffractive* processes have been analysed in hadron-hadron collisions in pre-HERA days. Diffractive events showed many features characteristic of optical diffraction and were described phenomenologically in the framework of Regge theory by the t-channel exchange of an object called *pomeron*. These ideas were successfully applied to diffractive events in photoproduction at fixed target experiments and at HERA.

Diffractive interactions at HERA are investigated both in inclusive and exclusive processes. The measurements deal with e.g. the diffractive structure function, the properties of the hadronic final state or the exclusive production of vector mesons. In the analysis of diffractive heavy vector meson production particularly two features provide an ideal testing ground for diffraction and for perturbative Quantum Chromo Dynamics (pQCD): On the one hand, only pomeron and no meson exchange occurs in J/ψ and Υ (as well as in φ) production. This is due to the different quark contents of these vector mesons and the proton (Zweig's rule). On the other hand, the large mass of the constituent quarks provides the hard scale needed for perturbative calculations. A significant amount of theoretical work has been carried out in the last years to understand charmonium production in the framework of QCD, where in a simple ansatz the pomeron is modelled as a system of two gluons.

Photoproduction of ρ mesons at HERA is measured to be well described by the same parameterization of the pomeron as extracted from total cross section measurements. For example the energy dependence of the ρ cross section (see figure 1.1) shows the $\sigma_{\gamma p} \propto W_{\gamma p}^{0.22}$ behaviour as predicted, with $W_{\gamma p}$ being the centre-of-mass energy of the photon-proton system. ω and φ photoproduction is not yet precisely measured at HERA energies. Nevertheless, it is found to be compatible with the Regge based models (see figure 1.1).

On the other hand, the energy dependence of the J/ψ photoproduction cross section is measured to be much steeper than in the case of the light vector mesons ($\sigma_{\gamma p} \propto W_{\gamma p}^{\sim 0.8}$, see figure 1.1).

This is interpreted as a signature for perturbative QCD mechanisms. Furthermore, the behaviour of the ρ production cross section in presence of a hard scale, such as the momentum transfer either at the electron vertex, Q^2, or at the proton vertex, t, shows the transition between the non-perturbative and the perturbative regimes. The study of diffractive J/ψ photoproduction might help to clarify the question, whether the high mass of the J/ψ alone – in absence of another hard scale – allows the application of perturbative calculations, or whether non-perturbative mechanisms are still important.

The subject of this thesis is diffractive J/ψ and Υ production, placing particular emphasis on the *elastic* processes, $ep \to eJ/\psi p$ and $ep \to e\Upsilon p$. In the case of Υ production the mass of the b quark should be large enough to allow the process to be fully calculable in perturbative QCD. The comparison of diffractive J/ψ and Υ meson photoproduction can therefore provide an additional probe of the transition region and the universality of the pQCD calculations for heavy vector meson production.

The focus of the measurements presented here is in particular the γp cross section of J/ψ and Υ mesons. The total cross section for elastic Υ meson production is measured, while the higher statistics for J/ψ allow one to study in detail the $W_{\gamma p}$ and the t dependences which can distinguish between the models assuming a pure soft process and the pQCD predictions.

Measuring the exchanged trajectory in terms of Regge theory is a very direct way to study whether elastic J/ψ photoproduction is driven by perturbative or non-perturbative mechanisms. The measurement as presented here is the first measurement of this kind using data from one single experiment only and therefore avoiding normalization problems and different treatment of the separation of the $\gamma p \to J/\psi p$ process from other, contaminating processes.

This thesis is organized as follows: In chapter 2 an introduction to HERA kinematics in general and the reconstruction of variables specifically important for this analysis are given. Afterwards the Monte Carlo generator programs used to correct the data for acceptance and efficiency losses are described. In chapter 3 the electron-proton accelerator HERA together with the main components of the H1 detector are discussed. In addition the trigger scheme as relevant for this analysis and two algorithms for muon identification are given. The identified muons are used to reconstruct the J/ψ via its muonic decay, $J/\psi \to \mu^+\mu^-$. The more technical part of the J/ψ analysis, namely the selection chain, efficiency studies and systematic errors, are discussed in chapter 4. The results on the $W_{\gamma p}$ and t dependence of the cross section, the $W_{\gamma p}$ dependence of the elastic slope parameter, the proton dissociative slope parameter and the exchanged Regge trajectory are presented and discussed in chapter 5. The results are compared with different theoretical predictions, shedding light on the question whether perturbative or non-perturbative effects are dominating.

The Υ photoproduction cross section measurement is performed in a similar way to the J/ψ analysis. However, some small changes are made to account for the different purity of the signal. The selection of Υ mesons, efficiencies and systematic errors are presented in chapter 6. The resulting γp cross section is compared to other measurements and to pQCD predictions. Finally, in chapter 7, an overall summary is given and conclusions are drawn.

In figure 1.1 the total photoproduction cross section, σ_{tot}, is shown, together with the cross sections of various vector mesons (ρ, ω, φ and J/ψ) in photoproduction, $\sigma(\gamma p \to Vp)$, for data from fixed target experiments and from HERA, including only results prior to the present analysis.

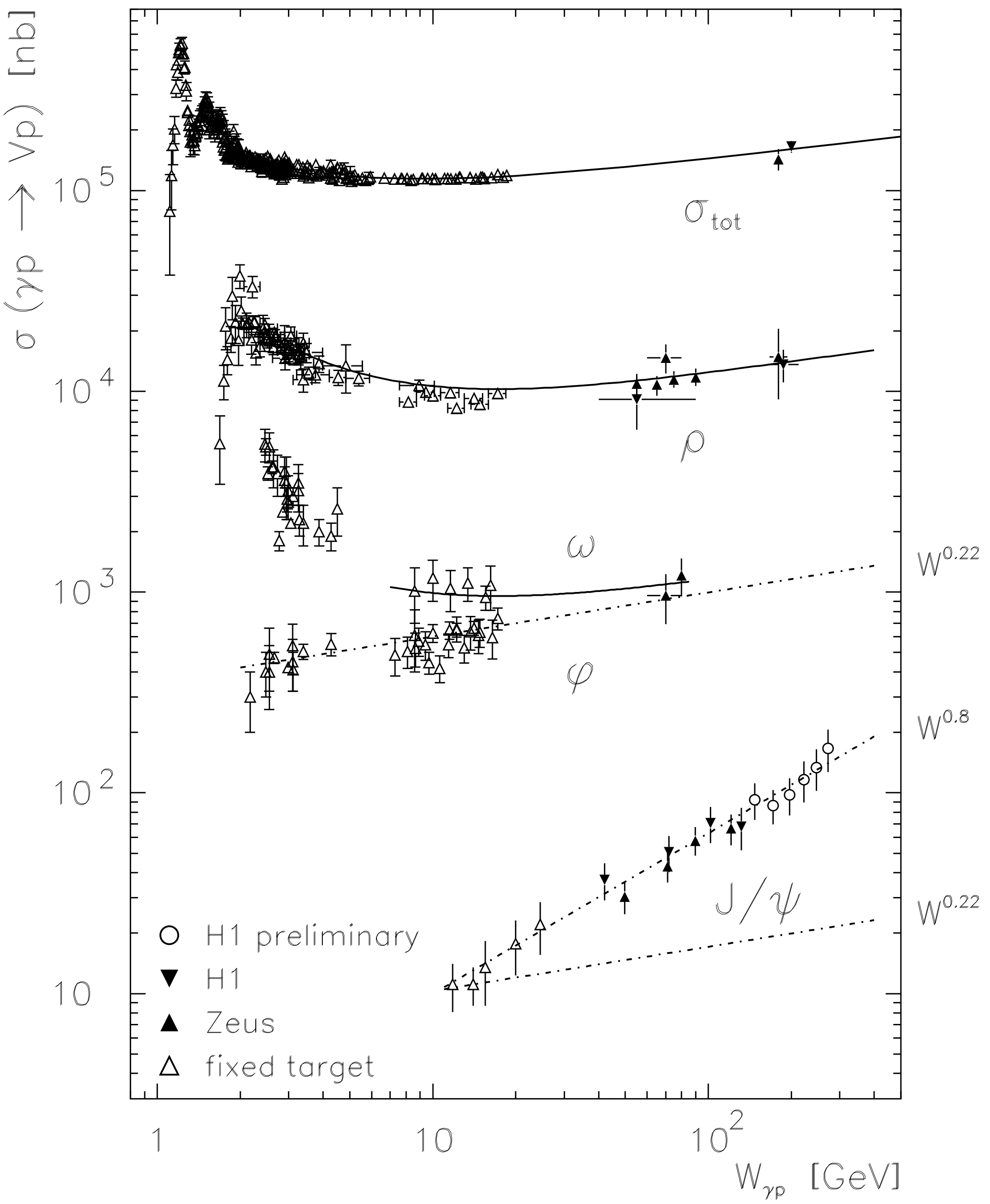

Figure 1.1: Compilation of $\sigma_{\gamma p}^{tot}$ and $\sigma_{\gamma p}$ for various vector mesons prior to the present analysis. The full lines are fits to the total photoproduction cross section, the elastic ρ, and the elastic φ cross section, using Regge parameterizations and assuming single pomeron exchange [1, 2]. The dashed lines visualize a certain energy dependence as indicated on the right hand side.

Chapter 2

Heavy Vector Meson Production

In this chapter, after a brief introduction of HERA kinematics, the diffractive production of heavy vector mesons is discussed in the light of several theoretical models. The basic ideas of these models are briefly explained and predictions for the behaviour of J/ψ and Υ cross sections as functions of kinematic variables are described. Finally Monte Carlo models, which are used to correct the data for acceptances and inefficiencies, are introduced. The term “diffractive” will be used in this thesis both, for pomeron exchange and for the event signature, which is determined by nothing but the decay leptons of the vector meson in the main detector. A more exhaustive overview of J/ψ history and physics can be found in [3] and [4] and of the specific subject of the pomeron in [5] and [6].

2.1 HERA Kinematics

In the basic deep inelastic scattering (DIS) process at HERA the incoming positron couples to an electroweak current, which probes the structure of the proton. Generic diagrams for a) neutral current (NC) and b) charged current (CC) processes are sketched in figure 2.1. The two processes

$$\text{a)} \quad e^{\pm}p \to e^{\pm}X \quad \text{(NC)} \qquad \text{and} \qquad \text{b)} \quad e^{\pm}p \to \nu_e(\bar{\nu}_e)X \quad \text{(CC)} \tag{2.1}$$

can be distinguished by the final state electron (NC) or neutrino (CC). Due to the high masses of the Z and W bosons, the exchange of photons is the dominant process. Z^0 exchange is suppressed by a factor $\sim Q^2/(Q^2+M_Z^2)$, and is therefore negligible in photoproduction ($Q^2 \approx 0$) and DIS at low Q^2. Also due to the propagator term charged current contributions are negligible.

With k and p being the four-momenta of the incoming lepton and proton and E_e and E_p their energies, the total centre-of-mass energy $\sqrt{s}$ is given by

$$s = (p+k)^2 \simeq 4 \cdot E_e \cdot E_p \tag{2.2}$$

neglecting the lepton and proton masses. The square of the four-momentum transfer at the electron vertex is given by

$$Q^2 = -q^2 = -(k-k')^2\,, \tag{2.3}$$

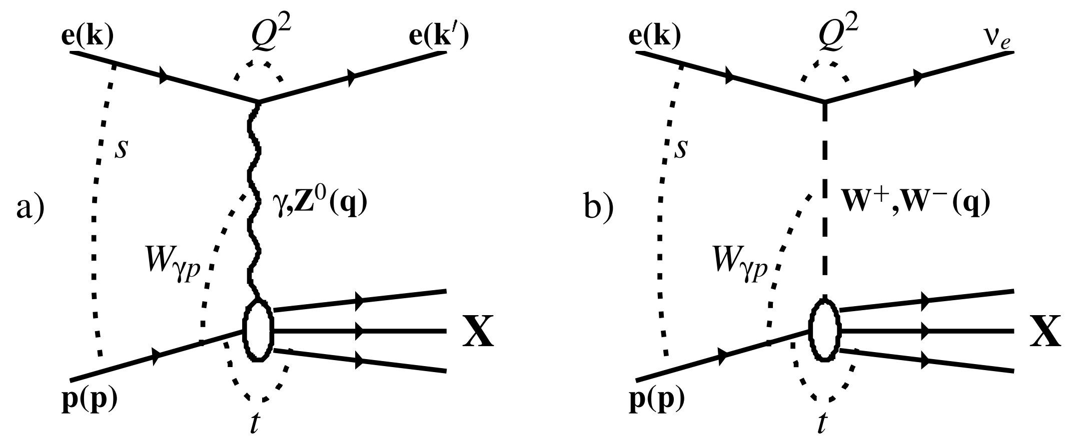

Figure 2.1: Generic graphs for *ep* collisions: a) neutral current (NC) and b) charged current (CC) deep inelastic *ep* scattering. The particles' four-momenta are given in brackets.

with q being the four-momentum of the exchanged gauge boson, and k and k' denoting the four-momenta of the incoming and scattered lepton.

At fixed centre-of-mass energy $\sqrt{s}$, the DIS process can be described by two Lorentz scalars. Choosing the dimensionless Bjorken scaling variable x and the inelasticity y as follows:

$$x = \frac{-q^2}{2 \cdot p \cdot q}, \tag{2.4}$$

$$y = \frac{q \cdot p}{k \cdot p}, \tag{2.5}$$

and neglecting the masses of the lepton and the proton, Q^2, x and y are related via

$$Q^2 = x \cdot y \cdot s\,. \tag{2.6}$$

x denotes the fraction of the proton momentum carried by the parton which couples to the electroweak current, and y corresponds to the fraction of electron energy transferred to the proton in its rest frame.

The square of the invariant mass $W^2_{\gamma p}$ of the hadronic final state X is related to x and Q^2 or y and Q^2 by momentum conservation at the proton vertex:

$$W^2_{\gamma p} = (p+q)^2 = Q^2 \cdot \left(\frac{1}{x} - 1\right) + m_p^2 = y \cdot s - Q^2 + m_p^2\,. \tag{2.7}$$

Three kinematic regions can be defined: for $x \to 1$ *elastic scattering* takes place ($W^2_{\gamma p} \to m_p^2$); in the limit $Q^2 \to 0$ almost real photons are radiated off the lepton defining the *photoproduction* region; while large Q^2 ($Q^2 \gtrsim 1\,\mathrm{GeV}^2$) and $W^2_{\gamma p} \gg m_p^2$ is the domain of *deep inelastic scattering*.

In the context of diffractive processes a further variable is introduced, the square of the momentum transfer at the proton vertex, t, which is defined as

$$|t| = (p - p')^2, \tag{2.8}$$

with p and p' denoting the four-momenta of the incoming and the scattered proton. In the case of diffractive vector meson production (see figure 2.2) t can be reconstructed via

$$|t| = -t_{min} + \overrightarrow{p_t}^2_{,p} \simeq (\overrightarrow{p_t}_{,e} + \overrightarrow{p_t}_{,V})^2 , \tag{2.9}$$

where $\overrightarrow{p_t}_{,p}$, $\overrightarrow{p_t}_{,e}$ and $\overrightarrow{p_t}_{,V}$ are the momentum components transverse to the beam direction of the final state proton, the positron and the vector meson. t_{min} is the minimal momentum transfer which is needed for the reaction to take place. With m_p denoting the proton mass, the minimal momentum transfer in the case of elastic vector meson production – i.e. the scattered proton stays intact – is given by

$$t_{min} = m_p^2 \left(\frac{Q^2 + M_V^2}{W_{\gamma p}^2} \right)^2 \simeq \left(\frac{M_V}{W_{\gamma p}} \right)^4 . \tag{2.10}$$

t_{min} is of the order of $10^{-6}(10^{-4})\,\mathrm{GeV}^2$ for J/ψ (Υ) photoproduction at $W_{\gamma p} = 100\,\mathrm{GeV}$.

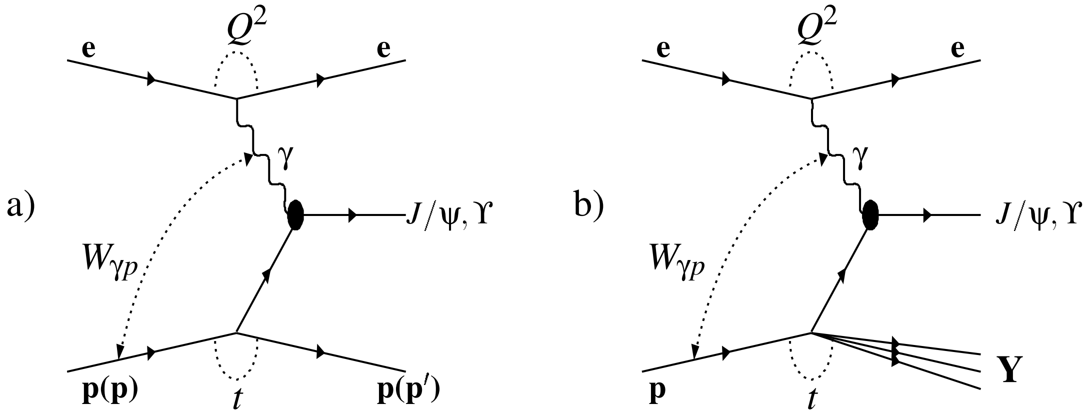

Figure 2.2: Generic graphs for a) elastic and b) proton dissociative vector meson production in ep collisions.

2.1.1 Photoproduction Regime

The analysis presented here is carried out in the *untagged* photoproduction regime ($Q^2 \lesssim 1\,\mathrm{GeV}^2$, $\langle Q^2 \rangle = 0.05\,\mathrm{GeV}^2$), i.e. the scattered positron is not measured in the detector. At such low momentum transfer Q^2 the electrons emit quasi-real photons, which then interact with the proton. The cross sections for the electroproduction ($ep \to eXp$) and the photoproduction ($\gamma p \to Xp$) processes are related via the improved Weizsäcker Williams Approximation (WWA) [7]-[10]. The electron–proton cross section σ_{ep} factorises into the photon–proton cross section $\sigma_{\gamma p}$ and the flux of transversely polarized photons Γ_T:

$$\sigma_{ep} = \int_{y_{min}}^{y_{max}} dy \int_{Q^2_{min}}^{Q^2_{max}} dQ^2 \cdot \Gamma_T(y, Q^2) \cdot \sigma_{\gamma p}(y, Q^2) \qquad \text{with} \tag{2.11}$$

$$\Gamma_T(y,Q^2) = \frac{\alpha_{em}}{2\pi y Q^2}\cdot\left(1+(1-y)^2 - 2m_e^2\frac{y^2}{Q^2}\right) \qquad \text{and} \tag{2.12}$$

$$Q^2_{min} = m_e^2\cdot\frac{y^2}{1-y}\,. \tag{2.13}$$

Defining the integrated flux of transversely polarized photons off the electron as

$$\mathcal{F} = \int_{y_{min}}^{y_{max}} dy \int_{Q^2_{min}}^{Q^2_{max}} dQ^2\cdot\Gamma_T(y,Q^2)\,, \tag{2.14}$$

a point $(\langle y\rangle, \langle Q^2\rangle)$ – or $(\langle W\rangle, \langle Q^2\rangle)$ – can be found for which

$$\sigma_{ep} = \mathcal{F}\cdot\sigma_{\gamma p}(\langle W\rangle, \langle Q^2\rangle) \tag{2.15}$$

is valid. Equation 2.15 is later on used to extract the photoproduction cross section from the measured electroproduction cross section in order to compare the measurement with theoretical predictions calculated for photoproduction processes.

2.1.2 Reconstruction of Kinematic Variables

The lack of knowledge about the scattered positron also influences the reconstruction of the momentum transfer at the proton vertex, t (compare equation 2.9). Due to the unmeasured $\vec{p_t}_{,e}$ only a rather poor resolution in t is achieved (see figure 2.3 b and e), while the reconstruction of $\vec{p_t}_{,V}$ is significantly better (see figure 2.3 a and d).

The reconstruction of the γp centre-of-mass energy, $W_{\gamma p}$, is performed with information from the hadronic final state only, the so-called Jacquet-Blondel [11] method. First y is reconstructed via

$$y = \frac{\Sigma_{had}(E-p_z)}{2E_e}\,, \tag{2.16}$$

where in the numerator the difference between energy and longitudinal momentum is summed for the hadronic final state, while the denominator contains twice the incoming electron beam energy (55 GeV). $\Sigma_{had}(E-p_z)$ is calculated from central tracks and cells in the liquid Argon (LAr) calorimeter and the backward calorimeter, a "spaghetti" type lead-scintillating fibre calorimeter (SpaCal). Tracks starting in inner Central Jet Chamber (CJC1) and fitted to the primary event vertex, with a relative error on the transverse momentum measurement $\sigma_{p_t}/p_t < 0.05$ and transverse momentum $p_t > 100\,\text{MeV}$, are taken into account assuming they are pions. For particles with transverse momenta above 300 MeV, energy deposits in calorimeter cells "behind" the tracks are ignored in order to avoid double counting. The hadronic final state mass $W_{\gamma p}$ is then calculated from y:

$$W_{\gamma p} = \sqrt{y\cdot s - Q^2 + m_p^2}\,. \tag{2.17}$$

The inelasticity y has a mean value of $\langle y \rangle \approx 0.07$ for elastic J/ψ events passing the selection chain described in chapter 4, and the mean Q^2 is $\langle Q^2 \rangle \approx 0.05\,\mathrm{GeV}^2$. The resolution in $W_{\gamma p}$ is shown in figure 2.3 c and f.

The quality of the kinematic reconstruction is displayed in figure 2.3, where reconstructed quantities after the full detector simulation (subscript "rec") are compared to the generated values (subscript "gen"), using the DIFFVM Monte Carlo program, which simulates diffractive J/ψ production (section 2.4.1). In figures a-c, the correlations between reconstructed and generated $p_{t,\psi}^2$, $|t|$ and $W_{\gamma p}$ are shown. In figures d-f the relative resolution in these three variables is given. It is about 16 % in $|t|$ and about 1 % in $W_{\gamma p}$. The quality of the $|t|$ resolution improves with $|t|$, from about 25 % for $|t| < 0.1\,\mathrm{GeV}^2$ to 14 % for $0.5 < |t| < 1\,\mathrm{GeV}^2$. The chosen bin sizes in the analyses later on will be at least two times larger than the resolution.

The hadronic final state mass $W_{\gamma p}$ and the polar angle of the vector meson are strongly correlated. This correlation is transferred to the vector meson's decay muons. In figure 2.4 the polar angle of the decay muons of J/ψ (top row) and Υ (bottom row) mesons is shown from simulated DIFFVM events. The ϑ_μ distributions are given for three different regions in $W_{\gamma p}$. The correlation between both variables can clearly be seen. The chosen acceptance range in the central part of the tracking system ($20^\circ \leq \vartheta_\mu \leq 160^\circ$ for J/ψ and $20^\circ \leq \vartheta_\mu \leq 165^\circ$ for Υ) is marked with vertical lines in each plot of figure 2.4. It limits the accessible range in $W_{\gamma p}$.

2.2 Regge Theory and the Vector Meson Dominance Model

Diffractive processes can be described within the framework of *Regge theory* [12, 13]. It is expected to be applicable if $W_{\gamma p}^2$ is much larger than any other scale involved, such as Q^2, t or quark masses. While Regge-inspired models [16, 17] are able to describe the total photoproduction cross section at HERA energies, discrepancies between the first HERA results on the proton structure function at very small x [14] and on elastic J/ψ photoproduction [15] and the predictions of the Donnachie-Landshoff [18] model based on Regge theory were found. In particular, in the case of J/ψ photoproduction, the energy dependence of the cross section is measured to be much steeper than predicted. Also no experimental evidence exists so far for the energy dependence of the elastic slope parameter, which defines the t dependence of the cross section, as postulated in the soft pomeron model by Donnachie and Landshoff. Models based on pQCD were discussed as an alternative.

The analysis presented here is performed in order to shed further light on the question of the importance of *soft* and *hard* mechanisms in diffractive J/ψ photoproduction. A process is said to be hard if it is driven by parton interactions and is at least in principle calculable in perturbative QCD. In this sense the Donnachie-Landshoff model is a soft model.

"Regge behaviour should not be understood as a substitute for perturbative QCD, but as a constraint on it, and an important task is to understand better how the two coexist." [19]

In the context of the Vector Meson Dominance Model (VDM, [20, 21, 22]) the photon is described as a quantum mechanical superposition of the bare QED photon state $|\gamma_{QED}\rangle$ and a hadronic state $|h\rangle$:

$$|\gamma\rangle = |\gamma_{QED}\rangle + |h\rangle\,, \qquad (2.18)$$

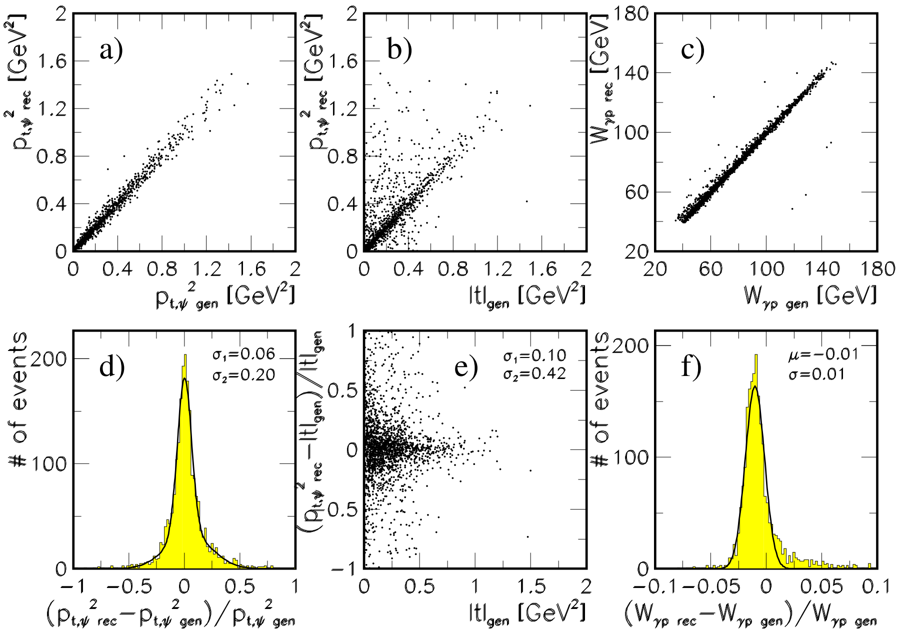

Figure 2.3: Reconstruction of kinematic variables determined from simulated DIFFVM J/ψ events, passing the selection chain described in chapter 4: the square of the transverse momentum of the J/ψ, $p_{t,\psi}^2$ (a,d), the momentum transfer at the proton vertex, $|t|$ (b,e) and the photon-proton centre-of-mass energy, $W_{\gamma p}$ (c,f). In the top row the correlation between generated and reconstructed variables is shown, while in the bottom row the resolution is shown together with the results from fitting one (f) or two (d,e) Gaussians to the data. In e) the resolution is displayed as a function of $|t|_{gen}$.

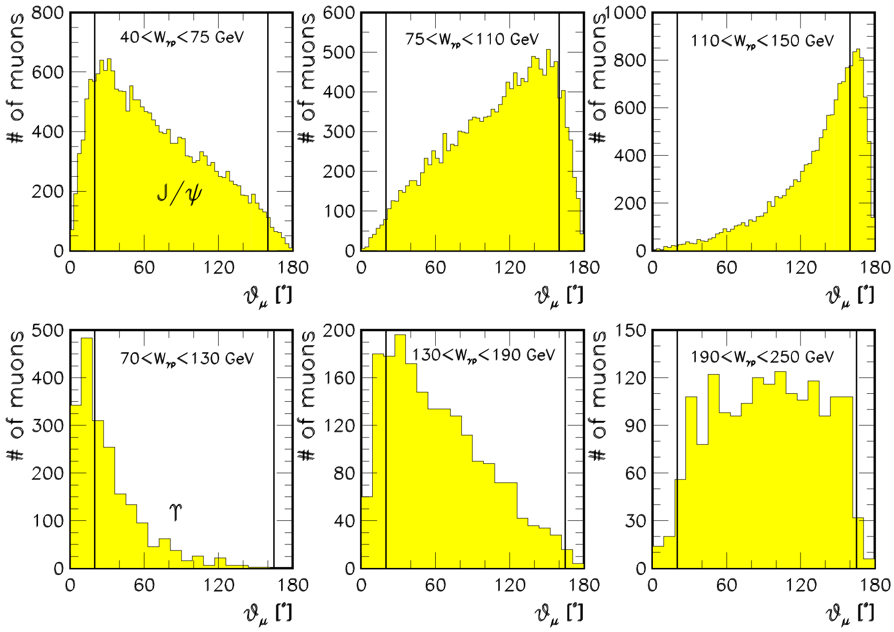

Figure 2.4: Correlation between $W_{\gamma p}$ and polar angle ϑ_μ for simulated elastic J/ψ events (DIFFVM) (top row) and Υ (bottom row) events. Shown is the polar angle of the decay muons for three different ranges in $W_{\gamma p}$. The vertical lines show the ϑ region analysed.

where $|h\rangle$ should have the same additive quantum numbers as the photon, which is the case for vector mesons ($J^{PC} = 1^{--}, Q = B = S = 0$):

$$|h\rangle = \sum \frac{e}{\gamma_V} |V\rangle\,, \tag{2.19}$$

with γ_V being the VDM coupling constant given by $(\frac{e}{\gamma_V})^2 = \frac{3\Gamma_{ee}}{\alpha_{QED} m_V}$, where Γ_{ee} and m_V are the electronic width and the mass of the vector meson. γ_V is assumed to be Q^2 independent and gives the probability for the transition of the photon to the vector meson. The justification for this picture was given by Ioffe [23], who argued that a photon can fluctuate also into a $q\bar{q}$ pair like it can fluctuate into an e^+e^- pair.

The sum in equation 2.19 is only performed over the diagonal elements ($\gamma^{(*)} \to V^{(*)} \to V$), neglecting off-diagonal contributions like $\gamma^{(*)} \to V^{(*)} \to V'$, where V' is a radially excited vector meson. These missing off-diagonal contributions are thought of as being responsible for the failure of VDM in the case of photoproduction of charmonium [24].

The idea of VDM as expressed in equation 2.18 is that the real and virtual photons fluctuate into a vector meson which then scatters off the proton (see figure 2.5). The proton can either stay intact (elastic vector meson production; figure 2.5 a) or dissociate (diffractive proton dissociation; figure 2.5 b). The transition between photon and vector meson is translated into the relation of the photon-proton cross sections:

$$\sigma(\gamma p \to V p) = \frac{4\pi\alpha_{QED}}{\gamma_V^2} \cdot \sigma(V p \to V p)\,. \tag{2.20}$$

For larger Q^2 values ($Q^2 \gtrsim m_V^2$) the vector meson propagator effect influences the photon proton cross section as follows:

$$\frac{\sigma^T_{\gamma p}(Q^2)}{\sigma^T_{\gamma p}(0)} = \frac{m_V^2}{m_V^2 + Q^2}\,, \tag{2.21}$$

$$\frac{\sigma^L_{\gamma p}(Q^2)}{\sigma^L_{\gamma p}(0)} = \xi \frac{Q^2}{m_V^2} \frac{m_V^2}{m_V^2 + Q^2} \tag{2.22}$$

for transversely and longitudinally polarized photons, respectively. The ratio of both contributions is then:

$$R(Q^2) = \frac{\sigma^L_{\gamma p}(Q^2)}{\sigma^T_{\gamma p}(Q^2)} = \xi \frac{Q^2}{m_V^2}\,, \tag{2.23}$$

where ξ is a phenomenological parameter of order 1, which takes into account that the Vp cross sections, σ_{Vp}, for transverse and longitudinal vector mesons could be different.

Within Regge theory diffractive processes at high energies are described by pomeron exchange. The characteristic of diffractive processes is the lack of colour flow between the scattered proton (or its dissociated remnant) and the hadronic final state (in this case the vector meson). This is explained by the exchange of a colourless object, the pomeron. These objects are thought of as being poles of the partial waves as a function of the momentum in the complex plane, all lying on linear trajectories in this plane. The poles are determined by the possible bound and resonant states [12]. The linear trajectories, $\alpha(t) = \alpha_0 + \alpha' \cdot t$, are each defined by a particular intercept, α_0, and a slope, α'.

In this picture the $W_{\gamma p}$ and t dependence of the J/ψ production cross section at high energy is determined by the intercept α_0 and the slope α' of the pomeron trajectory:

$$\frac{d\sigma_{\gamma p}}{dt} = \left.\frac{d\sigma_{\gamma p}}{dt}\right|_{t=0, W_{\gamma p}=W_0} \cdot e^{-b|t|} \cdot \left(\frac{W_{\gamma p}}{W_0}\right)^{4(\alpha_0 - 1)}, \tag{2.24}$$

with

$$b = b(W_0) + 2\alpha' \ln\left(\frac{W_{\gamma p}^2}{W_0^2}\right). \tag{2.25}$$

2.2.1 Soft Pomeron Model

In Regge theory, the elastic scattering process is described by the exchange of a superposition of Regge trajectories; the cross section is a sum of all contributions of each single trajectory. Since the cross section for the exchange of trajectories with an intercept smaller than one ($\alpha_0 < 1$) decreases with increasing centre-of-mass energy, at HERA energies only the pomeron trajectory ($\alpha_0 \gtrsim 1$) contributes in the case of vector meson production. The pomeron trajectory was postulated in 1961 [25] in order to describe the rise of the elastic and total cross sections measured in hadron-hadron scattering at large centre-of-mass energies. An intercept larger than one and vacuum quantum numbers ($I = S = B = 0, P = C = G = +$) were needed [13]. The new trajectory was called the pomeron, since a scattering process dominated by pomeron exchange fulfils the Pomeranchuk Theorem [26]; according to this theorem, the total cross section for the scattering

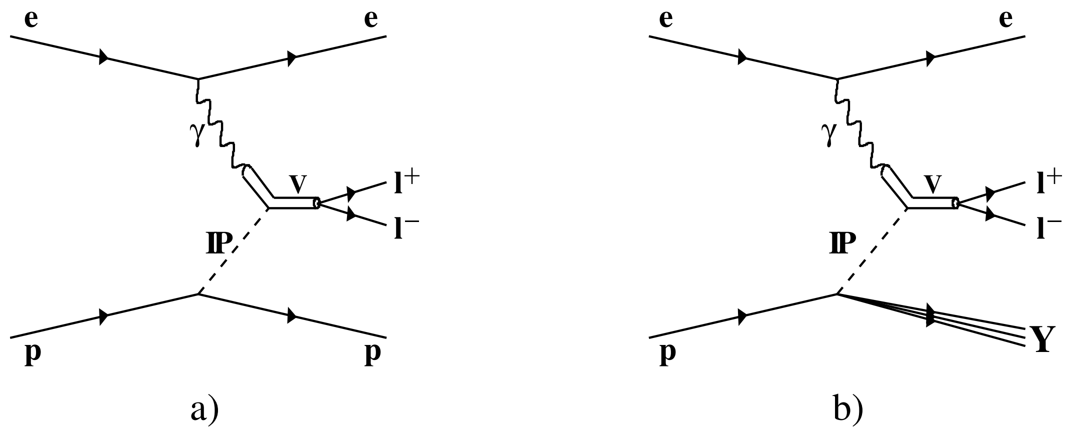

Figure 2.5: Vector meson production in Regge theory and the Vector Meson Dominance Model for a) elastic vector meson production and b) the proton dissociative process.

of particles and their anti-particles off a third particle should become equal at high energies. In contrast to those trajectories with an intercept of less than one (called reggeons), which can be related to observed particles (ρ, ω, f_2, a_2), no particle is known to lie on the pomeron trajectory[1].

Donnachie and Landshoff [17] performed a fit to $pp, \bar{p}p, \pi^- p, \pi^+ p, K^- p, K^+ p$ and γp data. They obtained a universal value for the intercept of the pomeron of

$$\alpha_0 = 1 + \varepsilon = 1.0808 \tag{2.26}$$

and a slope value of

$$\alpha' = 0.25\,\mathrm{GeV}^{-2}\,. \tag{2.27}$$

Together with the reggeon's intercept $\alpha_0 = 1 - \eta = 1 - 0.4525$ the energy dependence of all hadronic total cross sections and the total γp cross section can be parameterized as follows:

$$\sigma_{tot} = X s^{\varepsilon} + Y s^{-\eta}\,, \tag{2.28}$$

where the first term corresponds to pomeron and the second to reggeon exchange.

The main features predicted by the soft pomeron model of Donnachie and Landshoff are summarized in the following:

- From equation 2.24 follows an exponentially falling $|t|$ distribution, $\frac{d\sigma}{dt} \propto e^{-b|t|}$. The elastic slope parameter b can be interpreted as a geometrical measure for the size of the scattering objects in analogy to optical diffraction [27]: $b = (R_p^2 + R_V^2)/4$. With the proton radius $R_p \simeq 4\,\mathrm{GeV}^{-2}$ and measured elastic slope parameters in J/ψ production of $b \simeq 4-5\,\mathrm{GeV}^{-2}$, the J/ψ at HERA energies behaves almost point-like. This is not the case for ρ photoproduction ($b \simeq 10\,\mathrm{GeV}^{-2}$). The slope parameter for J/ψ production with proton dissociation is significantly smaller ($b \simeq 2\,\mathrm{GeV}^{-2}$).

- From equation 2.25: a non-universal, $W_{\gamma p}$ dependent elastic slope parameter, which increases logarithmically with energy. This effect is also known as *shrinkage* of the elastic (or forward) peak and provides a distinctive feature with respect to predictions within perturbative QCD, where b is thought of as being universal (see section 2.3).

- From equation 2.24 follows a slow increase of the cross section with energy, $\sigma_{\gamma p} \propto W_{\gamma p}^{0.22}$ ($\sigma_{\gamma p} \propto W_{\gamma p}^{0.32}$ without shrinkage). This is in strong contrast to the measured energy dependence of J/ψ production at HERA energies, $\sigma_{\gamma p} \propto W_{\gamma p}^{\sim 0.8}$ [15].

- In the case of proton dissociation, the same $W_{\gamma p}$ dependence of the cross section is expected as in the elastic case. In addition, the cross section is expected to fall like $1/M_Y^{2(1+\varepsilon)} \simeq 1/M_Y^2$ [27], with M_Y denoting the mass of the dissociated system, which is confirmed by experimental data [28].

[1] In [19] Donnachie and Landshoff fitted two 2^{++} glueball candidates to their *soft* and *hard* pomeron trajectories.

2.2.2 Two Pomeron Model

The data of various processes measured at HERA, such as the proton structure function F_2 for $x < 0.7$, the charm structure function and the elastic J/ψ photoproduction cross section deviate from the predictions of the soft pomeron model, but they are all in agreement with the assumption that there is a second pomeron, with an intercept of about $\alpha_{0_h} \simeq 1.4$. As one of the simplest assumptions, Donnachie and Landshoff [19] treat each of the two pomerons as a simple pole in the complex momentum plane, so that the contribution from each is a simple power of $W_{\gamma p}$ (or s, see equation 2.28). In addition to the two terms with powers ε and $-\eta$ in equation 2.28 a third term is added, which they call hard pomeron exchange (ε_h). Fits to γp cross section and F_2 data for $x < 0.07$ and $Q^2 < 10\,\mathrm{GeV}^2$ are performed yielding an intercept of the hard pomeron of $\alpha_{0_h} = 1 + \varepsilon_h = 1.418$. A systematic error on this result of about $\varepsilon_h \pm 0.05$ is estimated by the authors, preferring the upper end of this range as suggested by the presently available charm data ($F_2^{c\bar{c}}$).

Whatever the explanation of the hard pomeron might be, it is interesting that the mass scale that determines how rapidly its contribution to F_2 rises with Q^2, is considerably larger than the corresponding soft pomeron scale. Nevertheless, it may well be that even the hard pomeron is non-perturbative and that it is just a glueball trajectory [19]. The fact that the J/ψ photoproduction cross section rises much more steeply with energy than predicted by the soft pomeron model suggests that the slope of the hard pomeron trajectory may be small ($\alpha'_h \simeq 0.1\,\mathrm{GeV}^{-2}$). The resulting *hard* pomeron trajectory is then:

$$\alpha_h(t) \simeq 1.4 + 0.1 \cdot t\,. \tag{2.29}$$

2.2.3 BFKL Pomeron

Within the framework of the BFKL formalism a pomeron is postulated which is the perturbative QCD equivalent of the soft pomeron. An introduction to the BFKL formalism can be found elsewhere [30]. Here only the so-called BFKL pomeron [29] is introduced. It is an asymptotic ($x \to 0$) of the scattering amplitude in perturbative QCD in a certain kinematic region, where the logarithmic scale is large, $\alpha_s \ln(1/x) \gg 1$, and the virtualities of the incoming particles are more or less the same.

The highest eigenvalue of the BFKL equation is related to the intercept of the pomeron. In leading order (LO) it turns out to be rather large, $\alpha_{0_{BFKL}} = 1 + 12\,\ln(2\alpha_s/\pi) \simeq 1.55$ for $\alpha_s = 0.2$. Since the running of the QCD coupling constant α_s is not included and the allowed kinematic range of LO BFKL is not known, next-to-leading order (NLO) calculations are important. Recently the NLO corrections to the BFKL resummation of energy logarithms became available [31], and found to be large. Within non-Abelian physical schemes together with the BLM scale setting [32] the resulting NLO BFKL pomeron intercept is about $\alpha_{0_{BFKL}} \simeq 1.165$. In [29] no statement is made about the slope of the trajectory. For comparison with the data of this analysis it is assumed to be zero. The resulting BFKL pomeron trajectory is then:

$$\alpha_{BFKL}(t) \simeq 1.165\,. \tag{2.30}$$

2.3 Perturbative QCD Calculations

In perturbative QCD diffractive vector meson production is described by the exchange of a colourless two-gluon system (see figure 2.6) in leading logarithmic approximation (LLA), which uses the whole system of LLA ladder diagrams instead of the simple two-gluon pomeron. The amplitude is proportional to the gluon density in the proton, $\mathcal{A} \propto xg(x, Q^2_{eff})$, and the diffractive cross section to its square:

$$\sigma_{\gamma p} \propto [xg(x, Q^2_{eff})]^2 . \tag{2.31}$$

Therefore diffractive J/ψ production may be a good way to extract the gluon density in the proton as proposed by Ryskin in [33]. First attempts in leading order are described by using previous HERA and fixed target experiment results [34, 35]. But due to non-perturbative QCD effects, which are not yet under control, the related measurement is not performed in the present analysis.

Assuming that the exchanged pomeron is a gluon ladder (see figure 2.7), the transition from soft to hard processes can be understood within the following picture: During the trip from the virtual photon vertex down to the proton, the average transverse momentum, k_T, of the gluons gets smaller, the configuration larger, and at the proton vertex the low k_T region is reached governed by non-perturbative QCD. The average k_T of the partons in the process can be estimated by the slope of the exchange's trajectory since $\alpha' \propto 1/\langle k_T \rangle$. The question whether this transition is present might be answered by the determination of the pomeron trajectory in a given process. For a hard process $\alpha' \ll 0.25\,\mathrm{GeV}^{-2}$ would be expected [5].

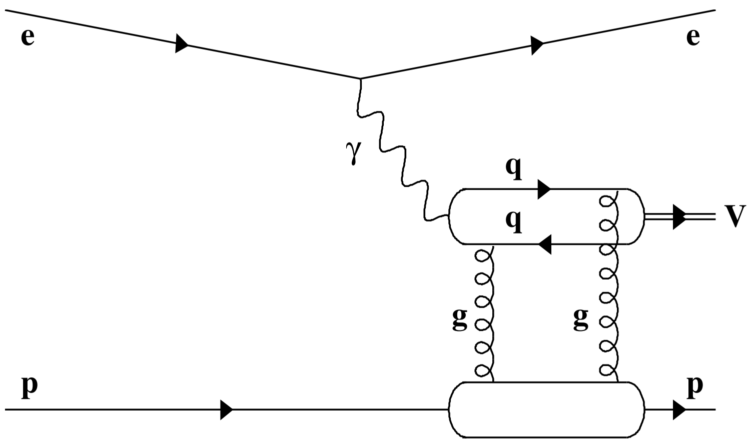

Figure 2.6: Leading order graph for elastic vector meson production in pQCD based models. Calculated, but not shown, are all four possible combinations of the two gluons coupling to the two quarks.

One basic concept of the description of diffractive vector meson production within perturbative QCD is the factorization of the process into three parts due to the QCD factorization theorem [36] and the large longitudinal coherence length associated with high energy (small x) diffractive processes [37, 38]:

- The fluctuation of the photon into a $q\bar{q}$ pair *long before* the interaction.
- The interaction between the $q\bar{q}$ pair and the proton on a *short* time scale ($x \ll 0.06$).
- The formation of the vector meson *long after* the interaction.

In order to apply perturbative QCD, the effective Q^2_{eff}, which provides the relevant scale in the process, has to be much larger than Λ_{QCD}. Therefore these calculations are applicable either in electroproduction at significant Q^2 values or, in photoproduction, for heavy vector mesons such as J/ψ, $\psi(2S)$ and Υ. While Ryskin has chosen Q^2_{eff} as $Q^2_{eff} = \frac{Q^2+m_V^2}{4}$, Frankfurt et al. have performed a rescaling, which leads to a significantly larger effective scale [39].

As shown in [38], for sufficiently large Q^2_{eff}, the process is dominated by $q\bar{q}$ configurations where the quark and antiquark are separated by a small transverse distance only. In the LLA only terms of the order $\alpha_s \ln(Q^2_{eff}/\Lambda^2_{QCD})$ are taken into account. The photon-proton cross section at $t = 0$ is in leading order [39]:

$$\left.\frac{d\sigma_{\gamma^{(*)}p}}{dt}\right|_{t=0} = \frac{12\pi^3\Gamma_{ee}m_V^3}{\alpha_{em}(Q^2+4m_q^2)^4} \cdot \left|\alpha_s(Q^2_{eff})(1+i\beta)xg(x,Q^2_{eff})\right|^2 \cdot \left(1+\varepsilon\frac{Q^2}{m_V^2}\right) \cdot C(Q^2), \quad (2.32)$$

where m_q is the pole mass of the quarks inside the vector meson (m_V), and x is given by

$$x = \frac{Q^2+m_V^2}{W^2_{\gamma p}}. \quad (2.33)$$

β denotes the relative contribution of the real part of the amplitude of the scattering of the $q\bar{q}$ pair off the parton in the proton:

$$\beta = \frac{\mathrm{Re}\mathcal{A}}{\mathrm{Im}\mathcal{A}} \simeq \frac{\pi}{2}\frac{\partial \ln(xg(x,Q^2_{eff}))}{\partial \ln x}, \quad (2.34)$$

which is small in case of J/ψ production, but of the order of one for Υ mesons. $C(Q^2)$ is a Q^2 dependent correction factor:

$$C(Q^2) = \left(\frac{Q^2+4m_q^2}{Q^2+4m_{run}^2}\right)^4 \cdot \left(\frac{\eta_V^2}{3}\right) \cdot \mathcal{T}(Q^2) \cdot \frac{\mathcal{R}(Q^2)+\varepsilon\frac{Q^2}{m_V^2}}{1+\varepsilon\frac{Q^2}{m_V^2}}. \quad (2.35)$$

Several Q^2 dependent corrections with respect to the asymptotic expression are taken into account in the term $C(Q^2)$:

- m_{run} is the running mass of the quarks in the vector meson, given by

$$m^2_{run}(Q^2_{eff}) = m_q^2\left(1 - \frac{8\alpha_s(Q^2_{eff})}{3\pi}\right). \quad (2.36)$$

- η_V is a leading twist correction, taking into account the difference between the vector meson *decaying* into an e^+e^- pair and diffractive vector meson *production*.

- $\mathcal{T}(Q^2)$ takes into account effects related to the Fermi motion of the quarks in the vector meson [38, 42].

- The factor $\mathcal{R}(Q^2)$ parameterizes the relative contribution of the production of transversely polarized vector mesons as compared to the naive prediction, and $\varepsilon = \frac{1-y}{1-y+y^2/2}$ is the polarization parameter ($\varepsilon = 1$).

The effective scale Q^2_{eff}, at which the gluons are sampled, is related to the dominant $q\bar{q}$ transverse distances in the respective quark loops. The value in J/ψ photoproduction, used in [39], is $Q^2_{eff} \simeq 5.1\,\mathrm{GeV}^2$. The corresponding scale for Υ production is significantly larger [43], see table 2.1.

	J/ψ	$\Upsilon(1S)$	$\Upsilon(2S)$	$\Upsilon(3S)$
Q^2_{eff} [GeV^2]	$\simeq 5.1$	$\simeq 40$	$\simeq 60$	$\simeq 75$

Table 2.1: Effective scales, Q^2_{eff}, for J/ψ, $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$ mesons, as used for cross section predictions in [39, 43].

The overall correction factor $\mathcal{C}(Q^2)$ for J/ψ photoproduction at HERA is of the order of $\mathcal{C}(Q^2) \simeq 0.1$ and $\mathcal{C}(Q^2) \simeq 0.5$ at $Q^2 = 100\,\mathrm{GeV}^2$. The largest single contribution is the Fermi motion suppression factor. While the influence on the cross section as a function of $W_{\gamma p}$ is mainly a change of the normalization, the Q^2 spectrum becomes significantly harder. In the case of Υ photoproduction the finite Q^2 correction factor is about $\mathcal{C}(Q^2 = 0) \simeq 0.3$, calculated with the same method as for J/ψ production (see figure 10 in [39]).

A large uncertainty in the prediction of the cross section is due to the uncertainty of the quark pole mass m_q. Varying m_q from $1.3 - 1.7\,\mathrm{GeV}$ changes the normalization of $\sigma_{\gamma p}$ by about a factor of two at $W_{\gamma p} = 90\,\mathrm{GeV}$. The choice of the gluon density function has a significant influence both on the shape and on the normalization of the cross section. In order to compare the measured J/ψ cross sections with the predictions later on (section 5), the cross section predicted by [39] is calculated for different parton densities, each adjusted by the choice of a certain charm quark pole mass, in order to fit the data in absolute magnitude.

In perturbative QCD models as presented here, a certain – but very weak – energy dependence of the slope parameter b is also predicted. Frankfurt et al. [39] find values for α' (see equation 2.25) of the order of $0.005 - 0.1\,\mathrm{GeV}^{-2}$ depending on x and t, which has to be compared to the larger value of $\alpha' = 0.25\,\mathrm{GeV}^{-2}$ in the case of the soft pomeron. They expect an elastic slope parameter $b = 4 - 5\,\mathrm{GeV}^{-2}$, almost independent of $W_{\gamma p}$.

2.3.1 Differences between J/ψ and Υ Production

When the first HERA results on diffractive Υ photoproduction became available [40, 41], the predictions based on the same assumptions as for J/ψ production [39] were about two standard deviations below the data. Since then, new calculations have been performed by two different groups [43, 44] taking into account mainly two novel effects, which turn out to be much more important than in the case of the J/ψ meson. On the one hand, the relative contribution of the real part of the amplitude is much larger for Υ than for J/ψ production, and on the other hand, the effect of skewed dynamics of the exchanged two-gluon system is more important for Υ mesons. Each effect accounts roughly for a factor of two in the cross section. In addition, a strong correlation between the mass of the vector meson and the energy dependence of the cross section is found. In particular, a considerably stronger rise with energy is predicted for Υ mesons ($\sigma_{\gamma p} \propto W_{\gamma p}^{\sim 1.7}$) than that found in J/ψ production ($\sigma_{\gamma p} \propto W_{\gamma p}^{\sim 0.8}$). Martin et al. [44] have also calculated a correction factor of 1.2 accounting for NLO effects [44].

Real Part of the Amplitude

At HERA energies Υ mesons are produced at large effective scales compared to J/ψ mesons (see table 2.1) and at relatively high x ($0.001 \lesssim x \lesssim 0.02$). Therefore the real part of the amplitude is large. It is calculated using a fit to the energy dependence of the imaginary part and dispersion relations. In the case of J/ψ production the ratio of real to imaginary parts of the amplitude, $\beta = \frac{\mathrm{Re}\mathcal{A}}{\mathrm{Im}\mathcal{A}}$, was calculated using the approximate solution of the dispersion relation (see equation 2.34). This is only appropriate at small x and fairly low scales, but in the case of Υ production it is necessary to include an additional sub-leading power in $1/x$ or equivalently in $W_{\gamma p}^2$. The effective difference between the recalculated β [43] and the one from equation 2.34 is given in table 2.2 as a function of $W_{\gamma p}$. It is most pronounced for smaller values of $W_{\gamma p}$.

$W_{\gamma p}$ [GeV]	80	130	180	230	280
β_{old}	0.94	0.82	0.77	0.75	0.73
β_{new}	1.12	0.87	0.79	0.74	0.71

Table 2.2: Contribution of the real part of the amplitude for $\Upsilon(1S)$ production for the CTEQ4L parton density at an effective scale of $Q^2_{eff} = 40\,\mathrm{GeV}^2$, calculated by Frankfurt et al. [43].

Martin et al. [44] give a correction factor on the cross section due to the real part of the amplitude of 1.43 at $W_{\gamma p} = 120\,\mathrm{GeV}$ and 1.36 at $W_{\gamma p} = 160\,\mathrm{GeV}$ for the MRS(R2) parton distribution.

Skewed Parton Densities

Recently, there has been considerable progress in calculating and understanding skewed parton distributions, which probe new non-perturbative information about hadrons and are a generalization of conventional parton distributions [45]. They are relevant for hard processes such as deeply virtual Compton scattering, diffractive photoproduction of dijets and photo- and electroproduction of heavy vector mesons.

The gluon emitted by the proton carries the proton momentum fraction x'' from the proton, while it has only the momentum fraction x with $x \ll x''$ when coupling to the quark. The returning gluon carries $x-\xi$ at the quark-gluon vertex and $x''-\xi$ at the proton-gluon vertex. Because the momentum fraction x and the difference in momenta of outgoing and returning gluon are of the same order of magnitude ($x \approx \xi$), the two gluons couple to the partons in the proton at different x values. With the coupling of the two gluons to the quark-antiquark pair, skewed parton density functions are probed at the vector meson level.

The skewedness, ξ, is given by the difference in momentum fractions carried by the outgoing (x) and returning ($x-\xi$) gluons (see figure 2.7), defined by:

$$x = \frac{m_{q\bar{q}}^2 + Q^2}{W_{\gamma p}^2 + Q^2}, \qquad x - \xi = \frac{m_{q\bar{q}}^2 - m_V^2}{W_{\gamma p}^2 + Q^2}, \tag{2.37}$$

$$\xi = \frac{m_V^2 + Q^2}{W_{\gamma p}^2 + Q^2}, \tag{2.38}$$

with $m_{q\bar{q}}$ denoting the mass of the intermediate $q\bar{q}$ state. From equation 2.38 the different influence of skewed dynamics in the case of J/ψ and Υ production can be seen ($\xi \propto m_V^2$). In the kinematic range of the analysis presented here, even though the mean $W_{\gamma p}$ value is much higher in the case of Υ production ($\langle W_{\gamma p}\rangle = 160\,\text{GeV}$) than for J/ψ ($\langle W_{\gamma p}\rangle = 90\,\text{GeV}$), the skewedness ξ is about a factor of two larger for Υ mesons. It is of the same order of magnitude as the momentum fraction x itself. For photoproduction at HERA, $\xi = \frac{m_V^2}{W_{\gamma p}^2}$ lies in the range $0.0011 \lesssim \xi \lesssim 0.017$ for Υ mesons and is about one order of magnitude smaller for J/ψ production.

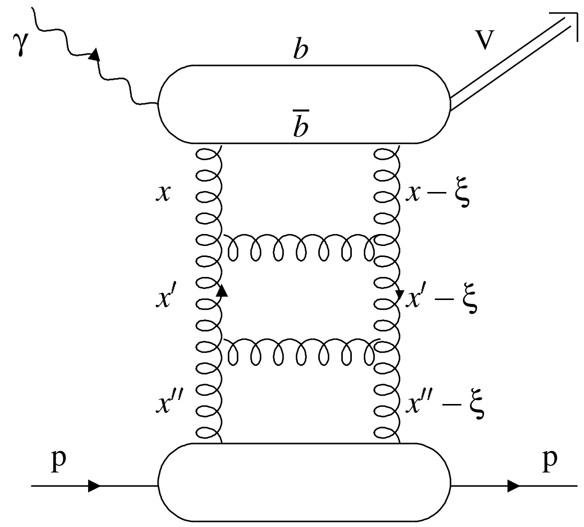

Figure 2.7: Diagram for the exchange of a gluon ladder.

Replacing the conventional gluon densities by the skewed distributions changes the cross section by an overall factor of about 2.6 (Frankfurt et al.) or 2.0 (Martin et al.), respectively. The correction is almost negligible for ρ production, and leads to about 10 % enhancement of the J/ψ amplitude [43], but is much more important for Υ photoproduction since the scale Q^2_{eff} and the value of x are much larger.

2.4 Monte Carlo Models

For the correction of the data, simulated events are used. The Monte Carlo generators deliver four-momenta of all particles in a given process with lifetimes longer than typically 8 ns. These generated events are tracked through the detector with help of a GEANT [46] based program. Then the detector and trigger response is simulated and finally the same reconstruction software as for real data is applied, taking detector noise into account by means of randomly triggered events from special runs. Two different Monte Carlo generators are used in the present analysis: DIFFVM for the simulation of elastic and proton dissociative J/ψ and Υ events and LPAIR, which simulates non-resonant QED lepton pair production. In this section both generators will be introduced and their physics input will be discussed.

2.4.1 DIFFVM

The DIFFVM [47] Monte Carlo generator was originally written to simulate diffractive vector meson production in ep scattering at HERA within the framework of Regge theory and the VDM (compare section 2.2). Both elastic and proton dissociative vector meson production can be simulated. Since many parameters can be adjusted freely, DIFFVM can be used as a largely model independent tool describing diffractive vector meson production which uses the basic ideas and terminology of Regge theory.

The emission of the photon from the incoming electron is treated within the equivalent photon approximation. Depending on y and Q^2, the angle and energy of the scattered electron are calculated. The emitted photon has a certain helicity, which is relevant for the angular distribution of the vector meson's decay particles and the Q^2 dependence of the cross section. Emission of additional photons (initial or final state radiation) is not implemented.

The transition of the photon to the virtual vector meson is modelled according to the VDM. The Q^2 dependence of the cross section for transversely polarized photons $\sigma^T_{\gamma p}$ is parameterized with

$$\sigma^T_{\gamma p} = \sigma_{\gamma p} \cdot \left(\frac{1}{1 + \frac{Q^2}{\Lambda^2}} \right)^n , \tag{2.39}$$

with the free parameters n and Λ. Within the VDM these two parameters are chosen to be $n = 2$ and $\Lambda = m_V$, where m_V is the mass of the produced vector meson. For longitudinally polarized photons the cross section $\sigma^L_{\gamma p}$ is given by

$$R(Q^2) = \frac{\sigma^L_{\gamma p}}{\sigma^T_{\gamma p}} = \frac{\xi \cdot \frac{Q^2}{\Lambda^2}}{1 + \chi \cdot \xi \cdot \frac{Q^2}{\Lambda^2}} , \tag{2.40}$$

where ξ is a constant factor of order 1, and χ is a purely phenomenological parameter, which limits R to the asymptotic value $1/\chi$ for $Q^2 \gg \Lambda^2$. For $\Lambda = m_V$ and $\chi = 0$ this reduces to

$$R(Q^2) = \xi \cdot \frac{Q^2}{m_V^2}, \tag{2.41}$$

and the cross section ratio is proportional to Q^2.

The dependence of the cross section on $W_{\gamma p}$ and t is parameterized according to Regge theory:

$$\frac{d\sigma}{dt} = \left.\frac{d\sigma}{dt}\right|_{t=0, W_{\gamma p}=W_0} \cdot e^{-b|t|} \cdot \left(\frac{W_{\gamma p}}{W_0}\right)^{4\varepsilon}, \tag{2.42}$$

with

$$b(W_{\gamma p}) = b(W_0) + 2\alpha' \ln\left(\frac{W_{\gamma p}^2}{W_0^2}\right), \tag{2.43}$$

where $b(W_0)$ is the slope parameter at some specific $W_{\gamma p}$, and $\varepsilon + 1$ and α' are the intercept and the slope of the exchanged pomeron trajectory. In the DIFFVM Monte Carlo generator, all these parameters can be chosen freely.

In the case of proton dissociative vector meson production, the cross section is proportional to $1/M_Y^{2(1+\varepsilon)}$, with M_Y being the mass of the dissociated system. In DIFFVM $1/M_Y^{2(1+0.08)}$ is used. Within the DIFFVM generator the dissociated system is treated as one of the nucleon resonances N(1440), N(1520), N(1680) or N(1710) for masses $M_Y < 1.9\,\text{GeV}$, which decay subsequently according to [48], while for larger masses a quark and a diquark are fragmented according to the Lund string fragmentation within the JETSET Monte Carlo program [49].

The main steering parameters which were used for event simulation in the present analysis are summarized in table 2.3.

	ε	n	Λ	ξ	χ	α'	b_{el}	b_{pd}
J/ψ	0.225	2.5	m_ψ	1.0	0.0	0.0	$4.0\,\text{GeV}^{-2}$	$1.6\,\text{GeV}^{-}2$
Υ	0.425	3.0	m_Υ	1.0	0.0	0.0	$4.0\,\text{GeV}^{-2}$	$1.6\,\text{GeV}^{-}2$

Table 2.3: Steering parameters used for J/ψ and Υ event simulation with the DIFFVM generator.

2.4.2 LPAIR

For the simulation of non-resonant background events the Monte Carlo generator LPAIR [50] is used. It generates elastic and proton dissociative events containing lepton pairs originating from multi-peripheral two-photon QED processes, $\gamma\gamma \to \mu\mu$, as sketched in figure 2.8 a and b respectively.

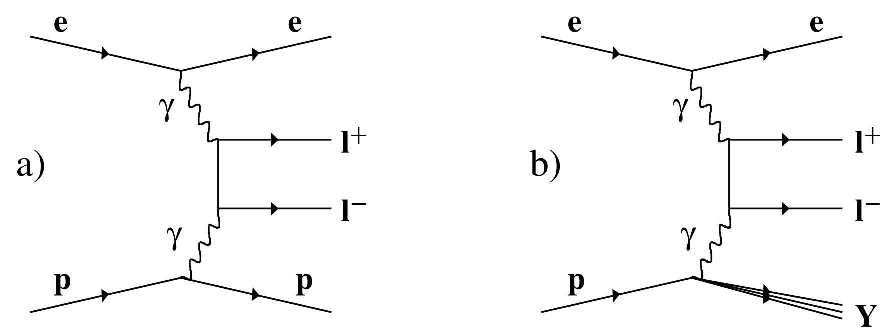

Figure 2.8: Graphs for QED two-photon processes as simulated with the LPAIR generator: a) elastic and b) dissociative multi-peripheral diagram for non-resonant lepton pair production.

These graphs describe the dominant source of background for diffractively produced J/ψ and Υ mesons. Further diagrams such as the Cabibbo-Parisi effect, the Compton-like or the Drell-Yan processes (see figure 2.9), in which the initial or final electron or one quark out of the proton radiates a photon, which then produces a lepton pair, are not considered in the LPAIR generator. Their contributions are expected to be negligible in the phase space covered by this analysis.

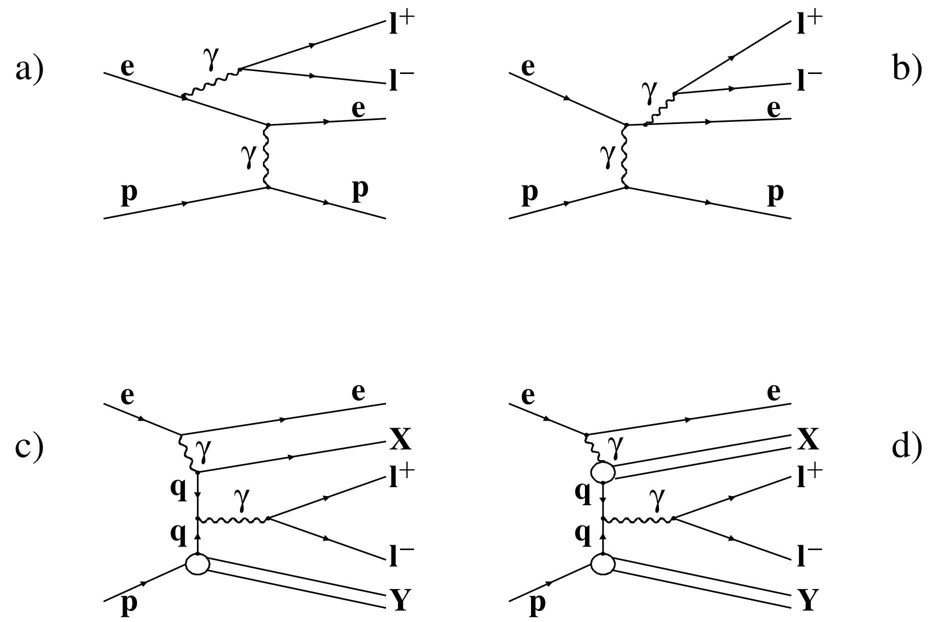

Figure 2.9: Graphs for QED two-photon processes not simulated with the LPAIR generator: a) Cabibbo-Parisi effect, b) Compton-like graph, c) point-like and d) resolved Drell-Yan process.

The LPAIR Monte Carlo is only used in the context of the b slope measurement. Since the t dependence of the QED two-photon cross section is steep compared to that of the J/ψ cross section, the simulated events are used to correct the t distribution for non-resonant background. In the case of the cross section measurement and the determination of the Regge trajectory the background is determined from the mass spectrum in the data without the need for simulated events.

Chapter 3

The H1 Detector at HERA

The data for this analysis come from e^+p collisions in HERA[1], at the DESY[2] laboratory in Hamburg. HERA collides positrons (or electrons) and protons at a centre of mass energy of 300 GeV. The data were collected by the H1 detector, a general purpose detector with almost hermetic calorimetry, precise tracking inside a solenoidal magnetic field, good lepton identification, and a fast four level trigger system. A detailed description of the H1 detector can be found elsewhere [51].

In this chapter the components of the experiment relevant for the present analysis are described, including the accelerator performance, tracking, calorimetry, and the muon and luminosity systems. The trigger chain and the two methods of muon identification used in subsequent chapters are also discussed.

3.1 Positron-Proton Collisions at HERA

A schematic overview of the HERA storage ring is shown in figure 3.1. Within two independent accelerators - one for protons and one for positrons - with a total circumference of 6.4 km, protons are accelerated up to beam energies of 820 GeV and positron beams are operated with 27.5 GeV. For the analysis presented here only positron-proton data are used from the years 1994 to 1997 in case of the Υ analysis and from 1996 to 1997 in case of the J/ψ analysis, respectively. In 1998 and 1999 electrons and protons have been collided and the proton beam was operated with 920 GeV. When the beams have reached their final energy, they are tuned to collide at very small angles in the interaction regions of the H1 and ZEUS experiments. The available centre-of-mass energy is $\sqrt{s} \approx 300$ GeV. This is one order of magnitude larger than the energies achieved so far in fixed target lepton-nucleon scattering experiments, and it is equivalent to a fixed target experiment operating with an electron beam of approximately 50 TeV.

The positron and proton beams are packed into 189 and 180 bunches, respectively, with a short bunch crossing interval of 96 ns (10.4 MHz). A small number of non-colliding bunches (*pilot*

[1]HERA=Hadron Electron Ring Accelerator
[2]DESY=Deutsches Elektronen Synchrotron

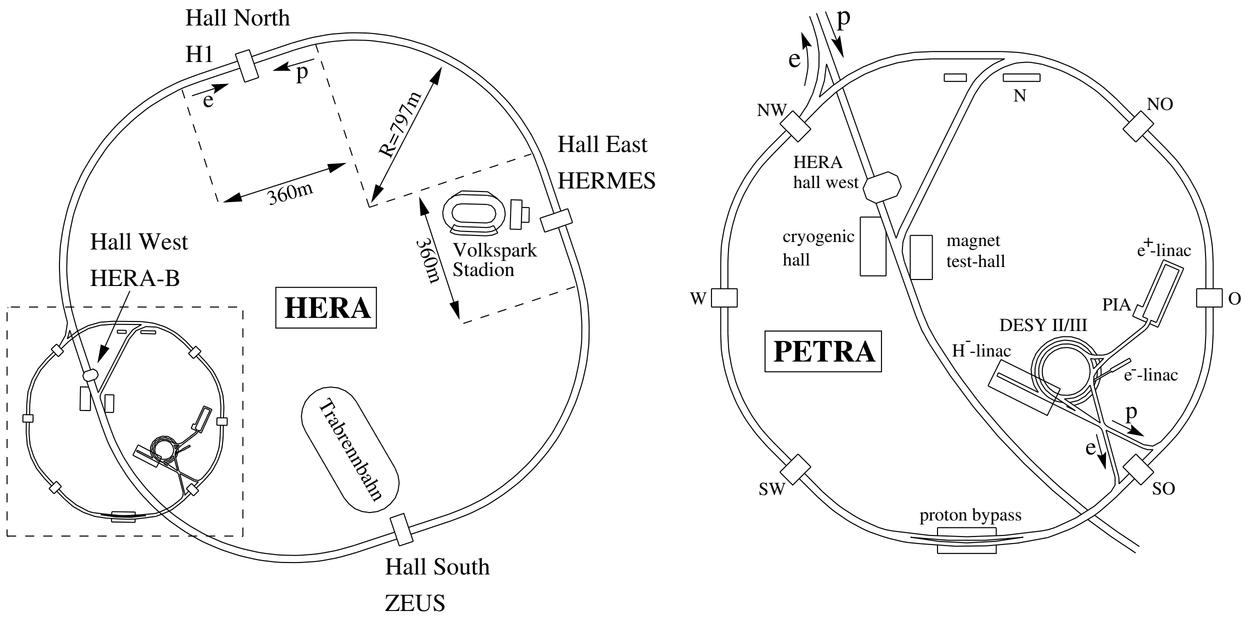

Figure 3.1: The storage ring HERA and its pre-accelerators at DESY. In addition the four experiments H1, ZEUS, HERMES and HERA-B are shown at the four interaction regions.

bunches) is usually preserved as a means of studying beam induced background arising from interactions of the beam with the residual gas in the beam pipe, or with its wall. The proton beam lifetime is rather large, of the order of 100 h, while the electron beam lifetime of about 10 – 20 h limits the typical duration of luminosity runs to less than 15 h. The integrated luminosity produced in the years 1992 to 1999 is shown in figure 3.2. The rise of the beam currents and HERA performance during the last years is clearly visible.

3.2 The H1 Detector

The H1 detector is a typical multi-purpose collider experiment consisting of several subdetectors. A specific feature of H1 is its enhanced instrumentation in the proton direction taking into account the asymmetric beam energies and boosted final states. A schematic view of the detector is shown in figure 3.3.

The main H1 detector has the approximate dimensions $12 \times 15 \times 10\,\mathrm{m}^3$ and weighs about 2800 t. The righthanded H1 coordinate system is shown in figure 3.3, it is chosen such that the z-axis is in the direction of the outgoing proton beam, called the forward direction.

3.2.1 Tracking System

The H1 tracking system consists of jet and drift chambers, multiwire proportional chambers as well as silicon detectors, which are integrated into a Forward Track Detector (FTD) and

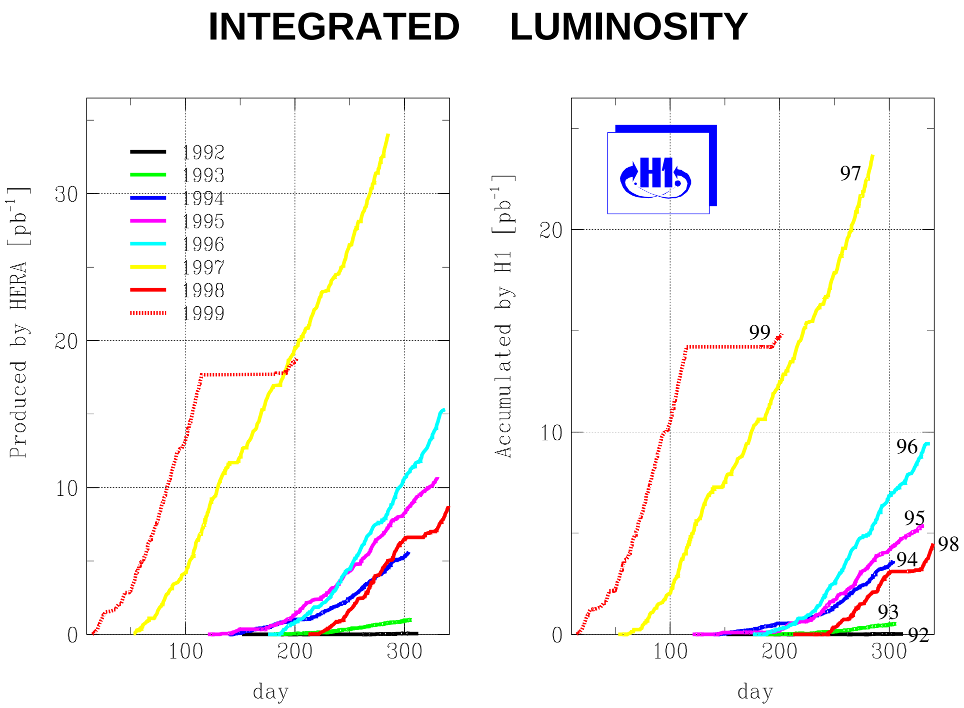

Figure 3.2: Integrated luminosity produced by HERA and measured in H1 for the years 1992-1999.

a Central Track Detector (CTD) (see figure 3.4). For this analysis only the CTD is used. It consists - radially from inside out - of the Central Silicon Tracker (CST), the Central Inner Proportional Chamber (CIP), the Central Inner z-Drift Chamber (CIZ), the inner Central Jet Chamber (CJC1), the Central Outer z-Drift Chamber (COZ), the Central Outer Proportional Chamber (COP) and the outer Central Jet Chamber (CJC2). While four of these chambers are used for track reconstruction (CJC1, CJC2, CIZ and COZ), the multiwire proportional chambers (CIP and COP) provide information for trigger purposes.

The six cylindrical chambers of the CTD are concentrically arranged in an aluminium tank. They provide a good momentum, angular and vertex resolution as well as a charge determination from the particle tracks. The CTD covers a polar angular range of $15° \lesssim \vartheta \lesssim 165°$.

Central Jet Chamber CJC

The track reconstruction in the central part of the H1 detector is performed using mainly the information of the inner and outer Central Jet Chambers (CJC1 and CJC2). CJC1 is built of 30 drift cells with 24 sense wires each, whereas CJC2 consists of 60 drift cells containing 32 sense wires each. The active length in z is 220 cm and the radial dimensions are 22.4 cm (CJC1) and 29.6 cm (CJC2) respectively.

The sense wires of the chambers are strung parallel to the beam axis (z-direction) to give accurate resolution in the $r\varphi$-plane. The drift cells are tilted by about 30° with respect to the radial direction (compare figure 3.5), so that the ionization electrons of high energy particles drift